

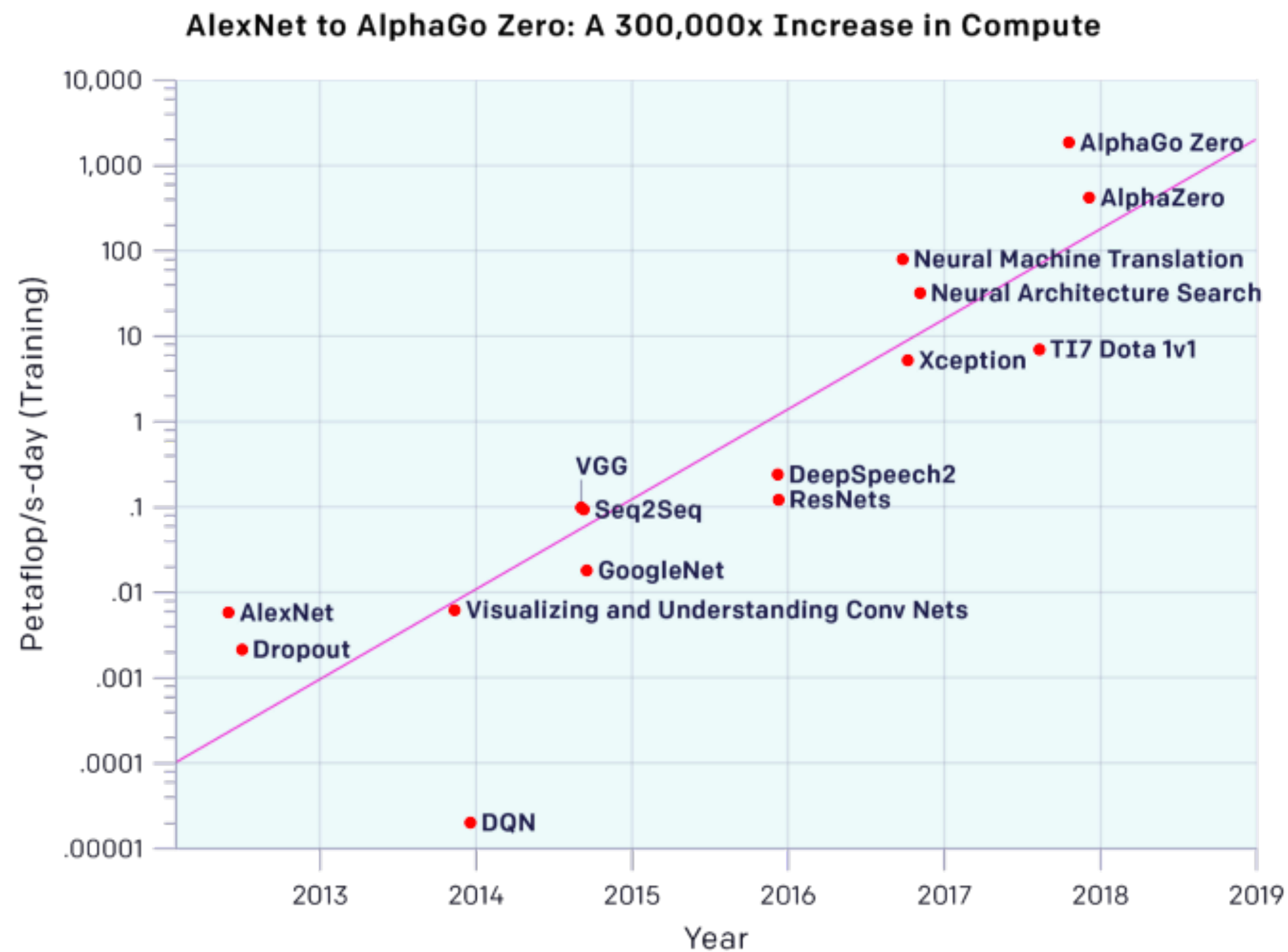
ML Systems Project

CS265 Spring 2025

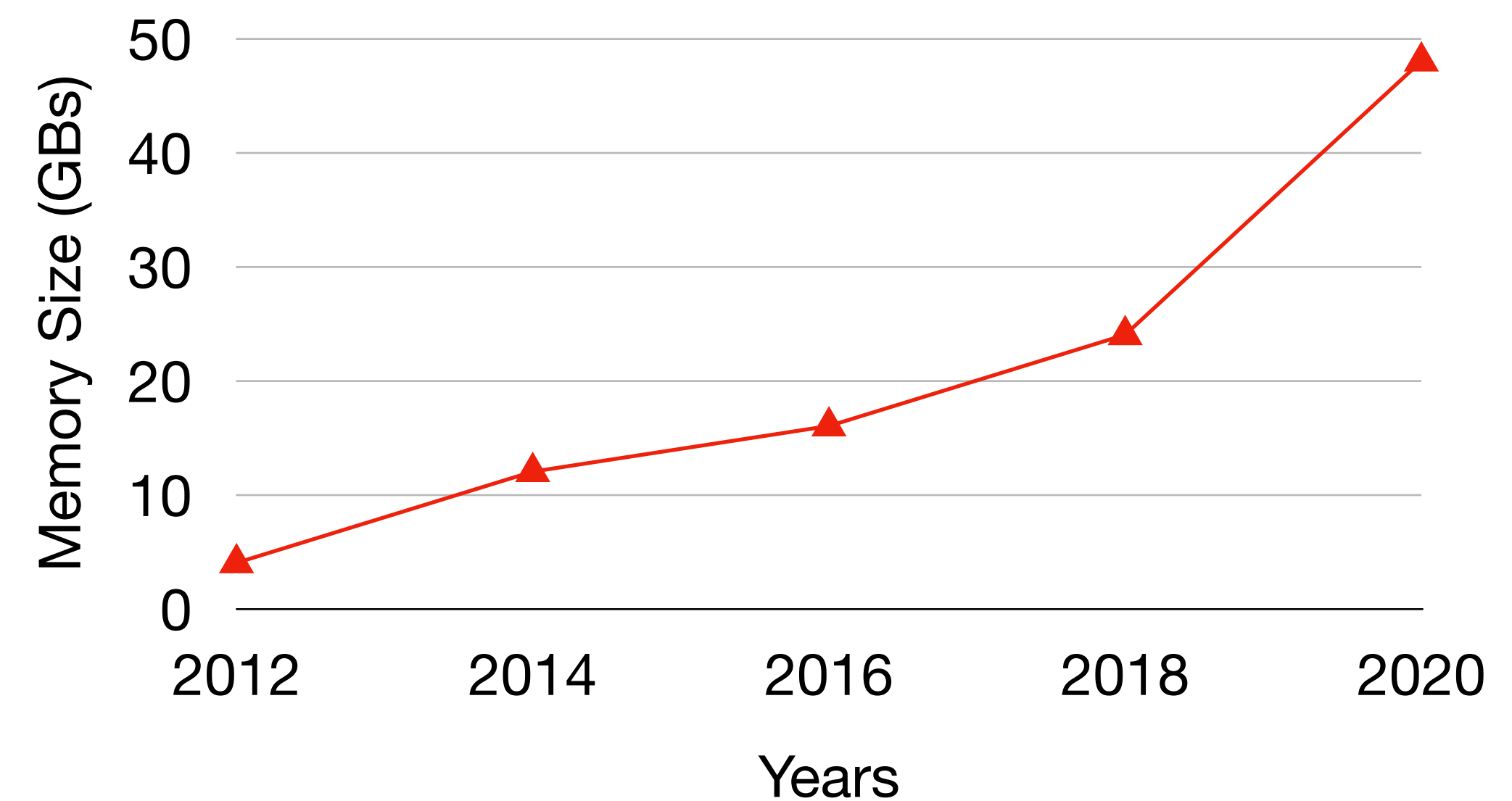


DASlab
@ Harvard SEAS

Memory is the Bottleneck in NN Training



Open AI: <https://openai.com/blog/ai-and-compute/>

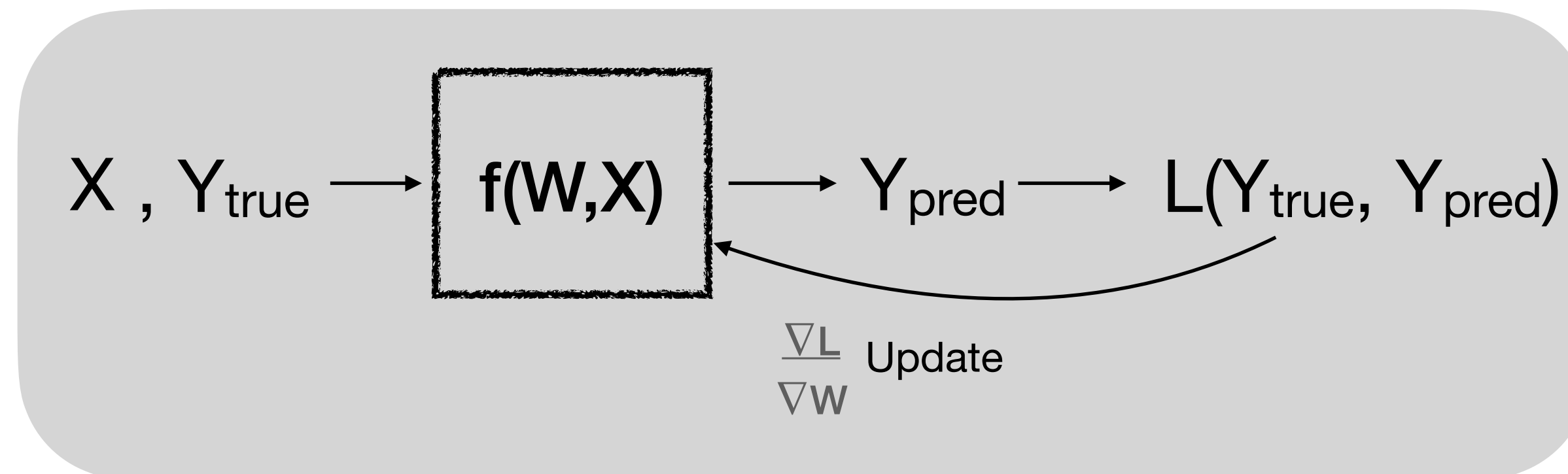


NVIDIA GPU Memory Sizes

Neural Network Training

Forward Pass

Black-box function: f
Input: X
Model Parameters: W



Loss Function: L
Prediction: Y_{pred}
True Label: Y_{true}

Loss (L): Distance from True Value

$\frac{\nabla L}{\nabla W}$: Gradient of Loss (L) wrt weights (W)

Forward Pass

Input X

$$Z_1 = W_1 X$$

$$Z_2 = \sigma(Z_1)$$

$$Z_3 = W_3 Z_2$$

$$Z_4 = \sigma(Z_3)$$

$$L = \frac{1}{2}(Z_4 - Y)^2$$

True Label Y

$$W_i = W_i - \alpha \nabla W_i$$

Update Rule

Function Composition

$$y = f(x) \quad \frac{\delta z}{\delta x} = \frac{\delta g(y)}{\delta y} \frac{\delta y}{\delta x}$$

$$z = g(y)$$

$$z = g(f(x)) \quad \frac{\delta z}{\delta x} = \frac{\delta g(f(x))}{\delta f(x)} \frac{\delta f(x)}{\delta x}$$

Chain Rule

Backward Pass

$$\nabla W_1 = \nabla Z_1 X$$

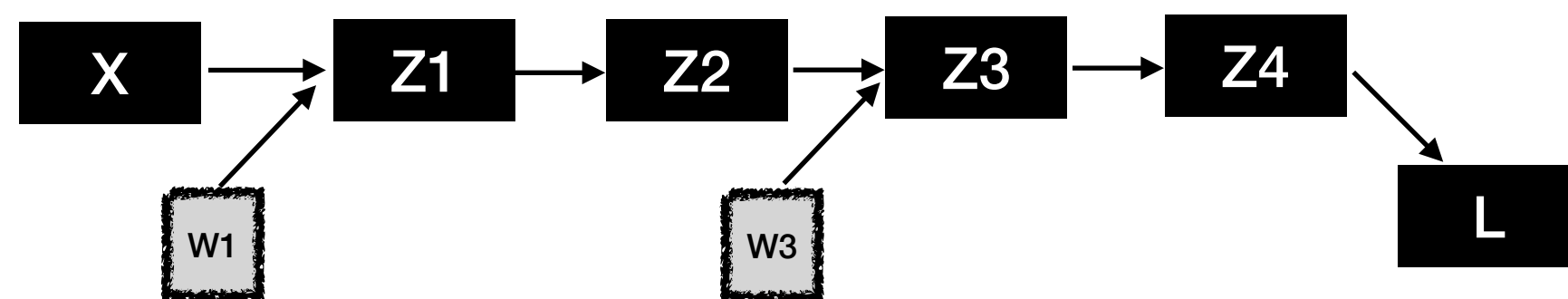
$$\nabla Z_1 = \nabla Z_2 Z_2 (1 - Z_2)$$

$$\nabla Z_2 = \nabla Z_3 W_3$$

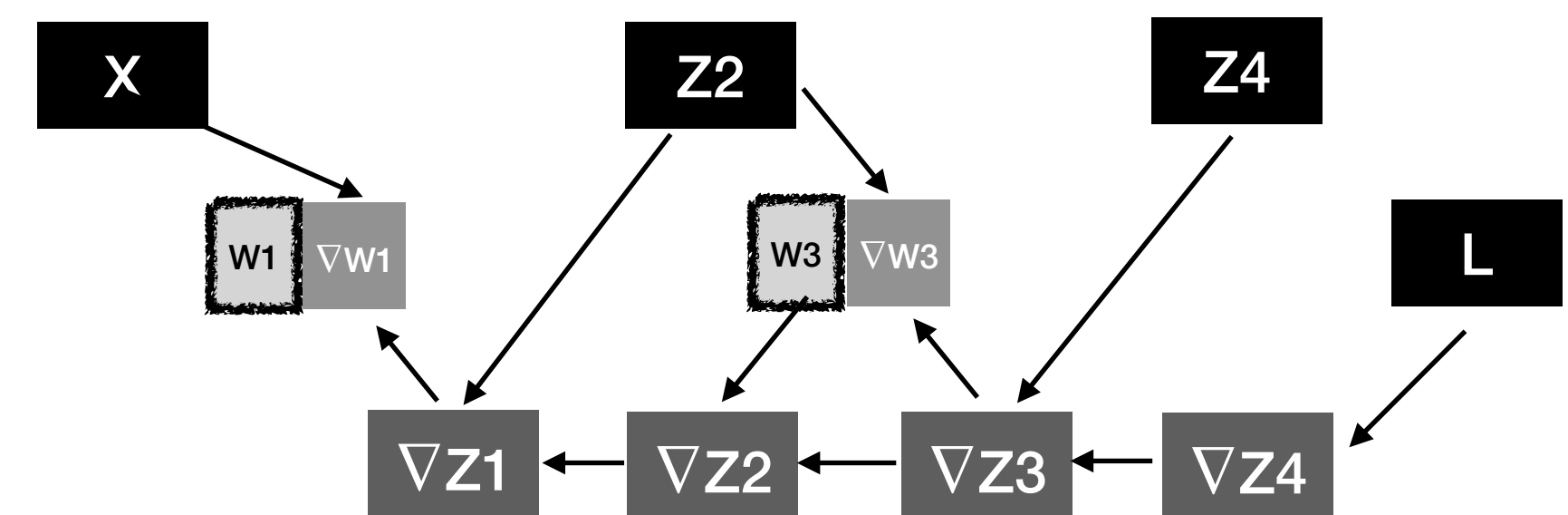
$$\nabla W_3 = \nabla Z_3 Z_2$$

$$\nabla Z_3 = \nabla Z_4 Z_4 (1 - Z_4)$$

$$\nabla Z_4 = (Z_4 - Y)$$



Forward Computational Graph



Backward Computational Graph

Forward Pass

Input X
 $Z_1 = W_1 X$
 $Z_2 = \sigma(Z_1)$
 $Z_3 = W_3 Z_2$
 $Z_4 = \sigma(Z_3)$
 $L = \frac{1}{2}(Z_4 - Y)^2$
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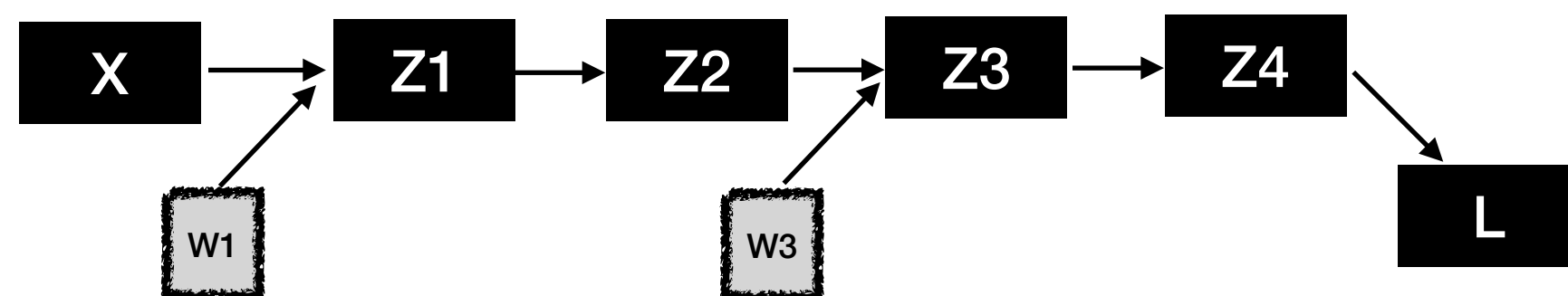
Update Rule

Legend

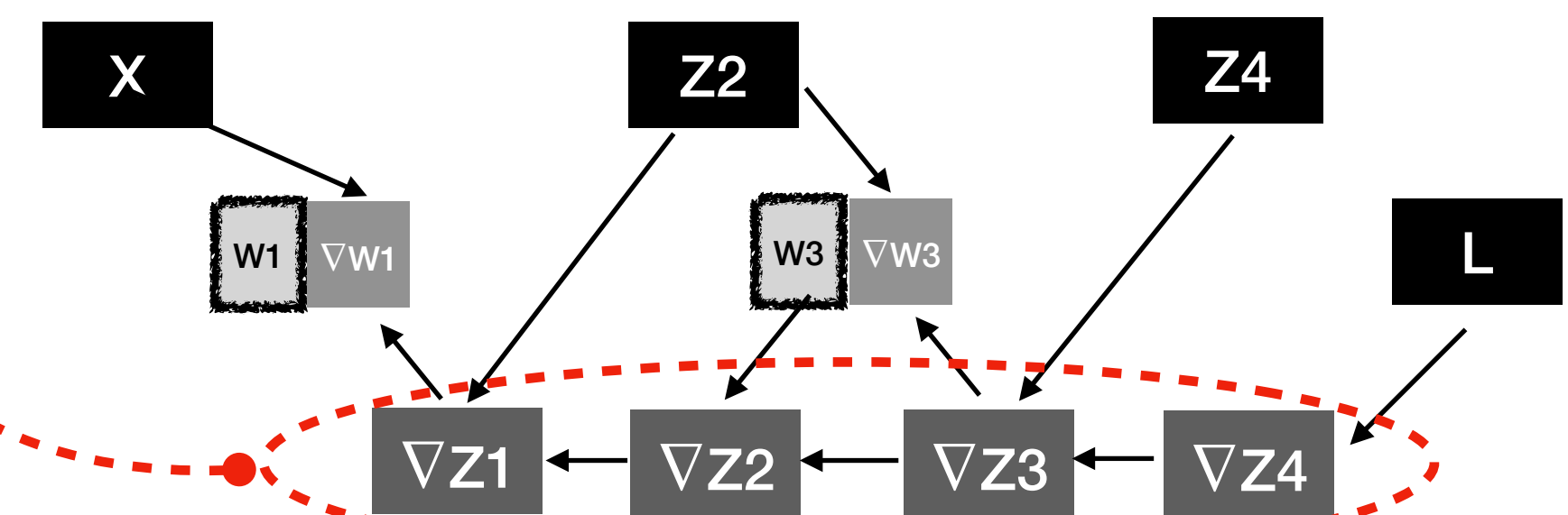
Z1	Activation/Feature Maps
W1	Weight/parameter
∇W_1	Weight Gradient
∇Z_1	Gradient Maps

Backward Pass

$\nabla W_1 = \nabla Z_1 X$
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Forward Computational Graph



Backward Computational Graph

Forward Pass

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Update Rule

Legend

- Z1** Activation/Feature Maps
- W1** Weight/parameter
- ∇W_1** Weight Gradient
- ∇Z_1** Gradient Maps

Backward Pass

$$\nabla W_1 = \nabla Z_1 X$$

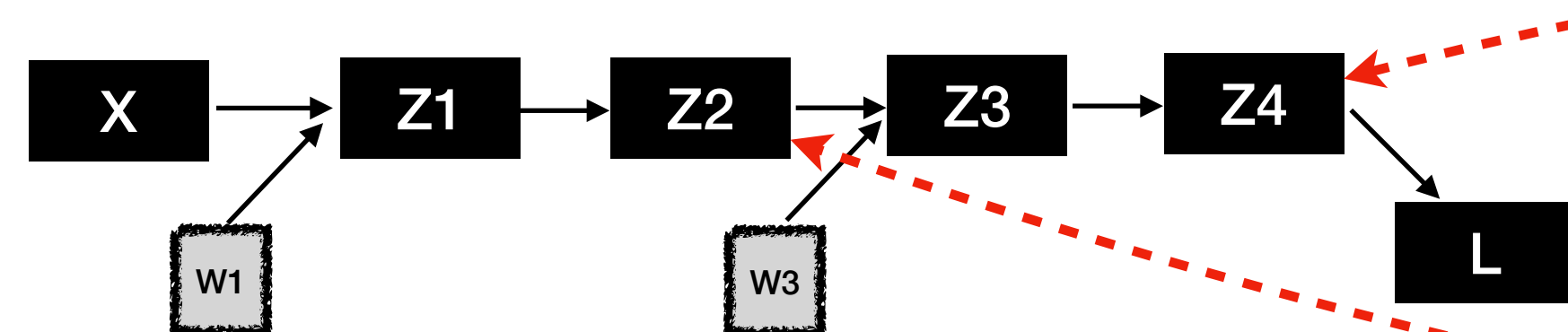
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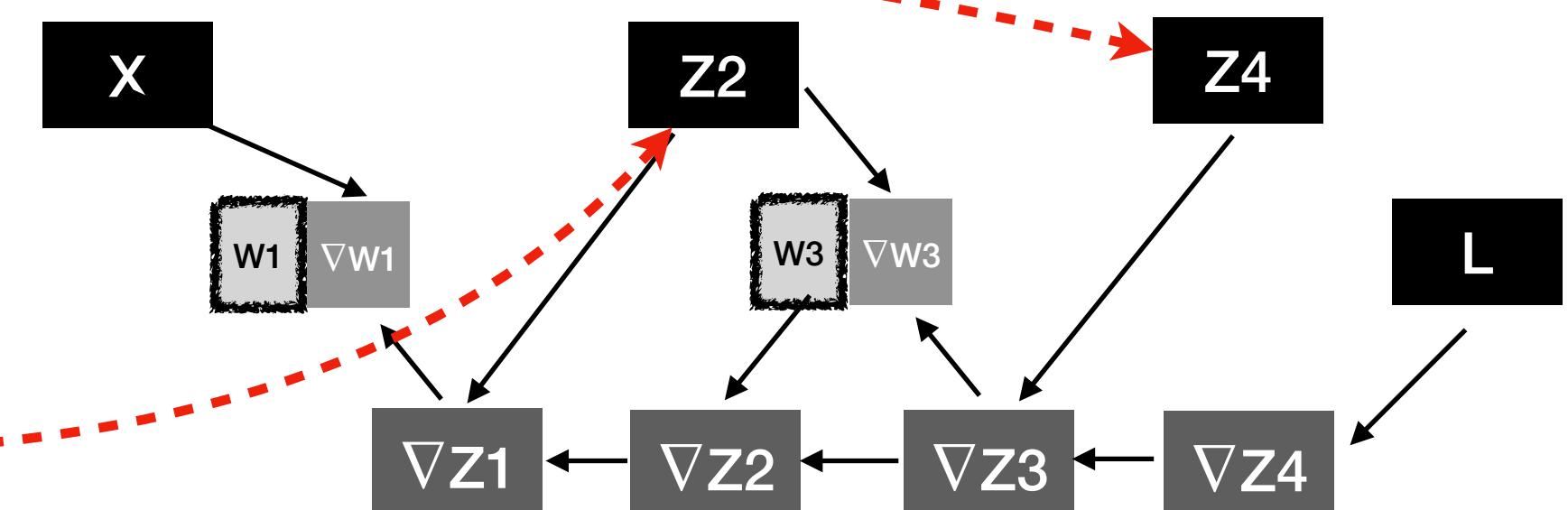
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Forward Computational Graph



Backward Computational Graph

Forward Pass

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Update Rule

Legend

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W1 Weight/parameter
 ∇W_1 Weight Gradient
 ∇Z_1 Gradient Maps

Backward Pass

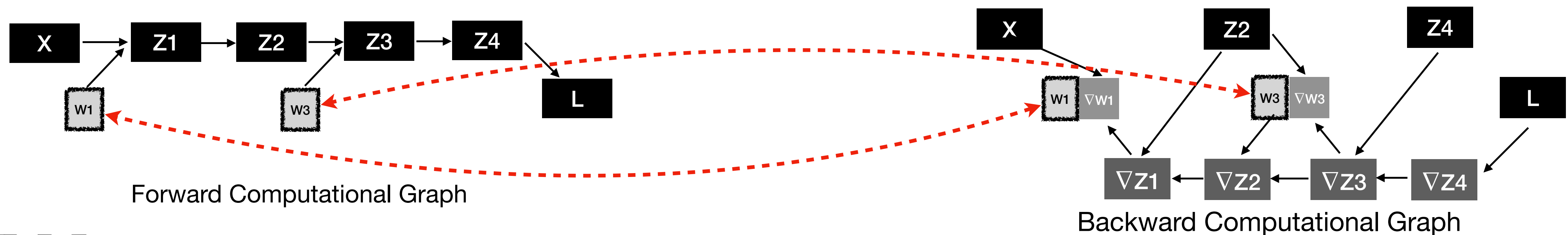
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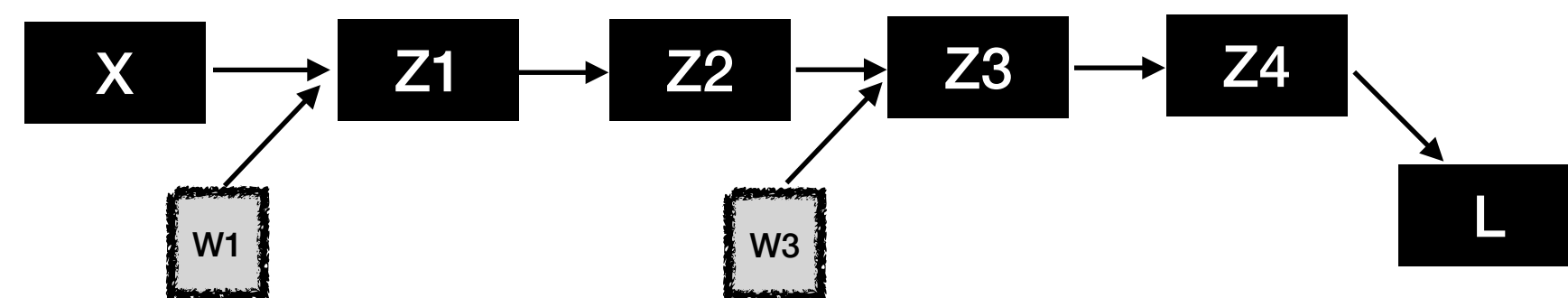
Update Rule

Legend

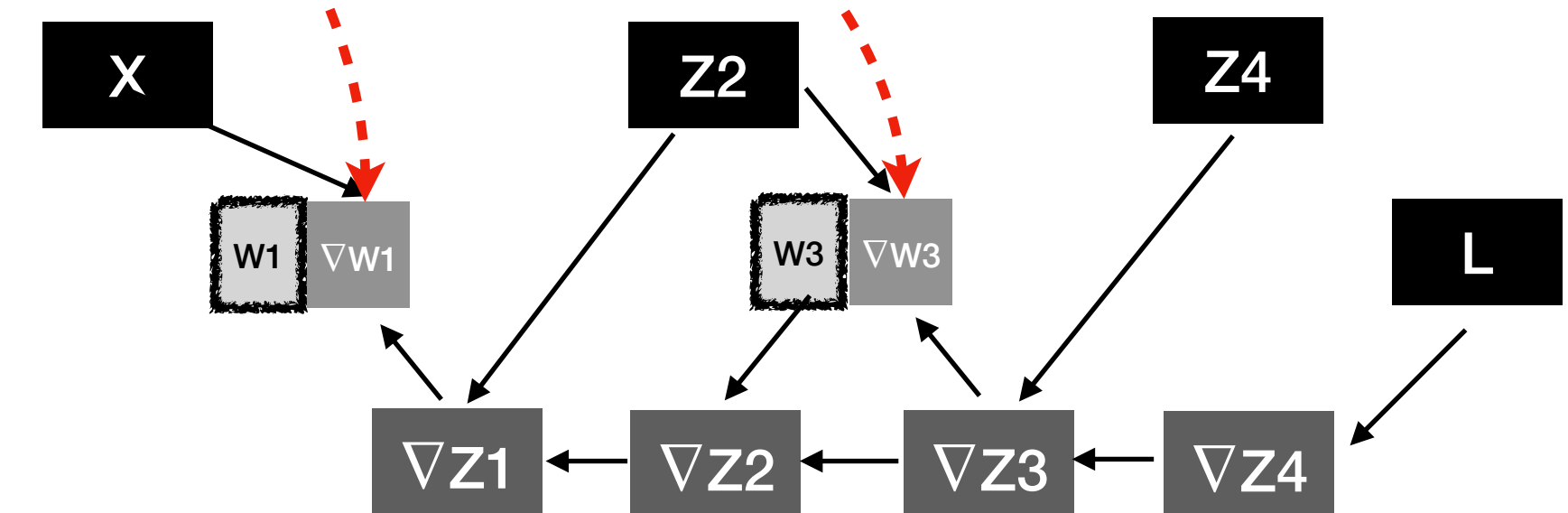
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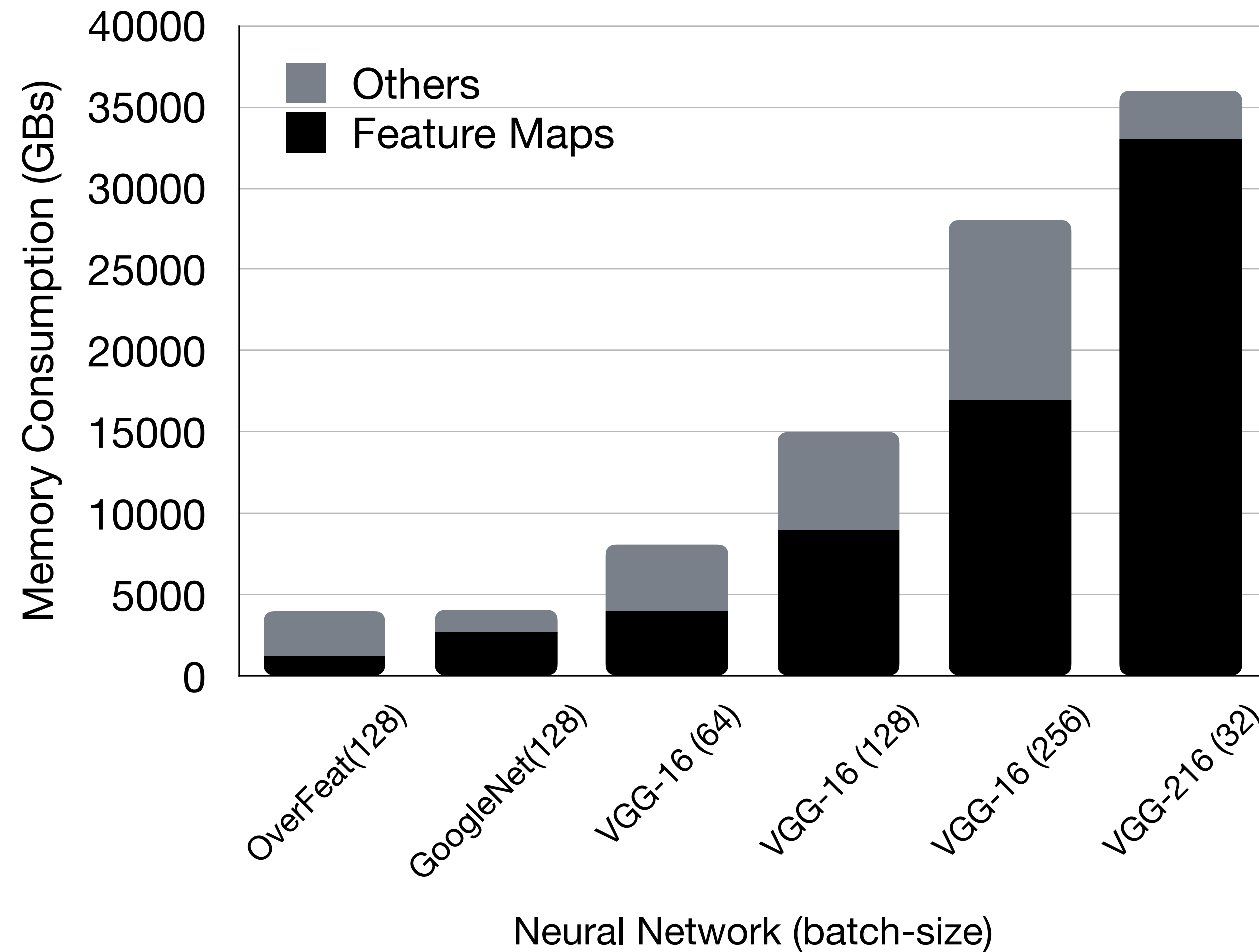


Forward Computational Graph

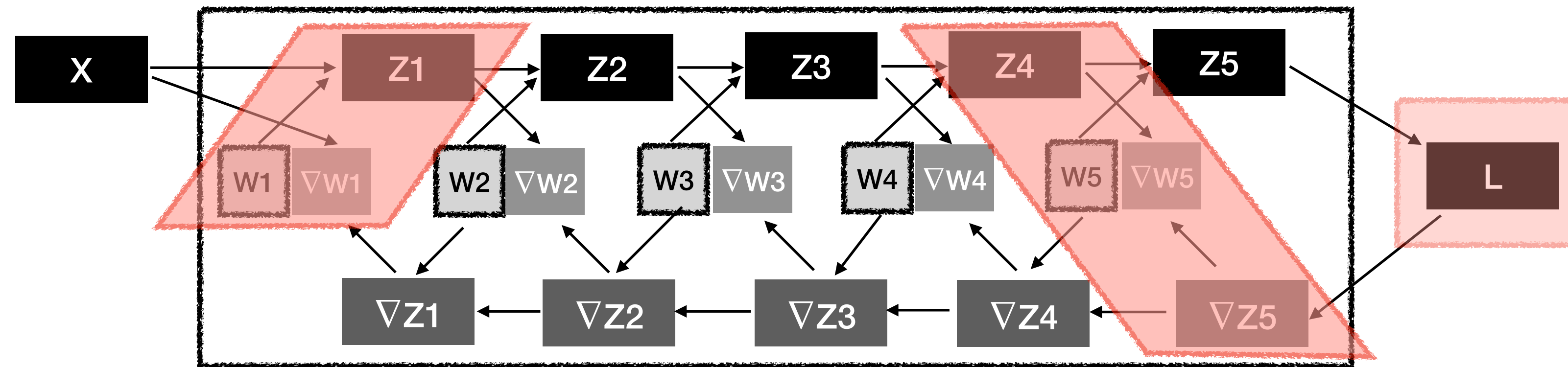


Backward Computational Graph

Reduce Memory Footprint



Execution Framework



Computation Graph

Forward Pass
Operation Time



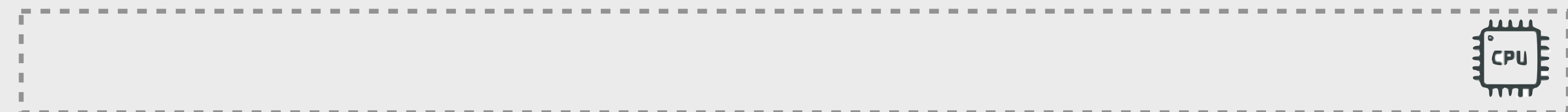
Backward Pass
Operation Time



Execution Timeline



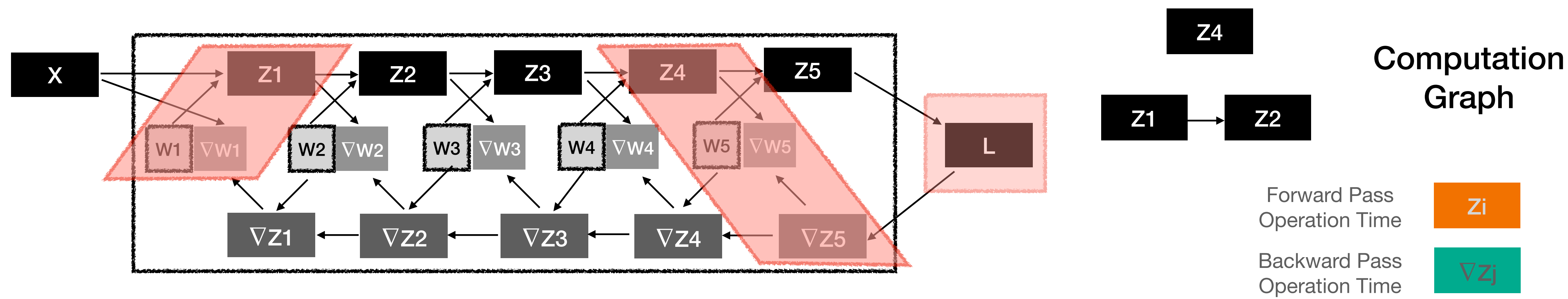
GPU Memory



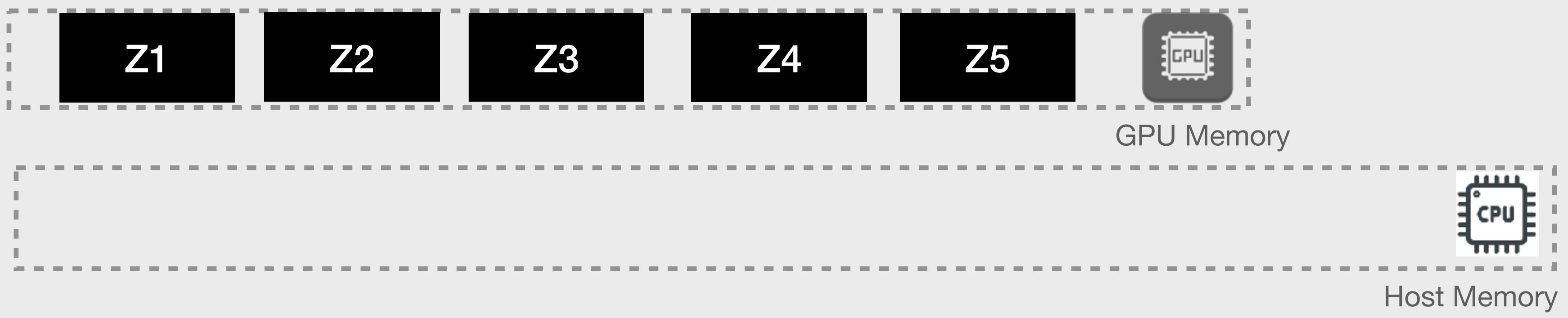
Host Memory

Memory Content

Activation Checkpointing



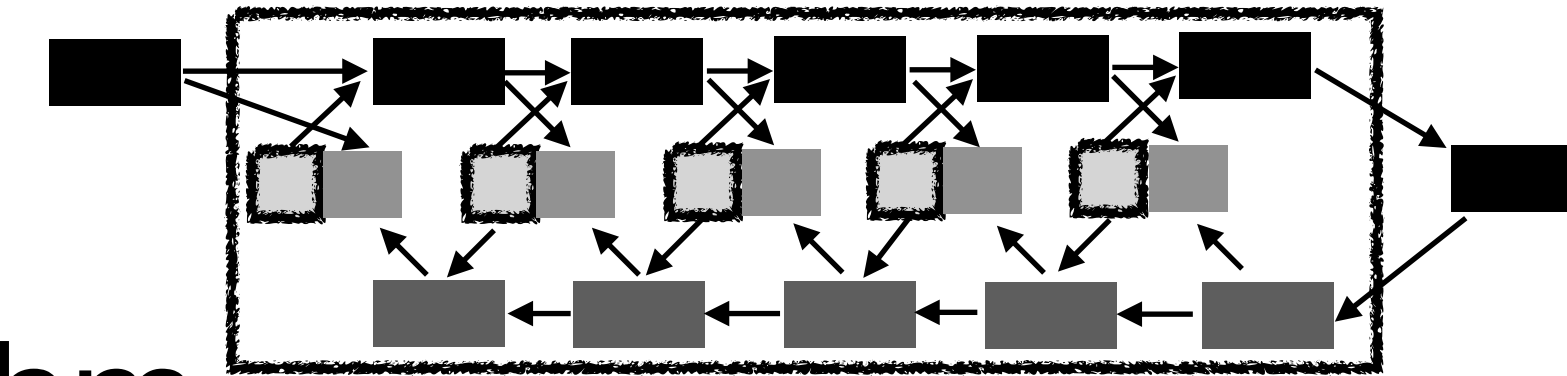
Discard



Memory Content

The ML Systems Project

1. construct and profile the computational graph on PyTorch



2. design the activation checkpointing (AC) algorithm

3. rewrite the PyTorch computational graph to deploy activation checkpointing

http://daslab.seas.harvard.edu/classes/cs265/files/CS_265_Systems_Project_Description.pdf

How to Start

1. play with the starter code (instructions in README.md)

<https://github.com/qtwang/CS265-mlsys-project>

2. check the reference paper

Sanket Purandare, Abdul Wasay, Animesh Jain, Stratos Idreos: μ -TWO: 3 $\times$ Faster Multi-Model Training with Orchestration and Memory Optimization. MLSys 2023.

3. come to the labs with questions!

Midway Check-in

1. complete Phase 1: construct and profile the computational graph
2. a document with experimental analysis consisting of the following two deliverables:
 - computation and memory profiling statistics and static analysis
 - peak memory consumption vs. mini-batch size bar graph without AC

Final Deliverables

1. code deliverable + code review + demo = 50%
2. a document with experimental analysis = 50%
 - computation and memory profiling statistics and static analysis
 - peak memory consumption vs mini-batch size bar graph (w and w/o AC)
 - iteration latency vs mini-batch size performance graph (w and w/o AC)

Enjoy!